

Lesson 8: Estimating Quantities

Classwork

Exercise 1

The Federal Reserve states that the average household in January of 2013 had \$7,122 in credit card debt. About how many times greater is the US national debt, which is \$16,755,133,009,522? Rewrite each number to the nearest power of 10 that exceeds it, and then compare.

Exercise 2

There are about 3,000,000 students attending school, kindergarten through 12th grade, in New York. Express the number of students as a single-digit integer times a power of 10.

The average number of students attending a middle school in New York is 8×10^2 . How many times greater is the overall number of K-12 students compared to the number of middle school students?

Exercise 3

A conservative estimate of the number of stars in the universe is 6×10^{22} . The average human can see about 3,000 stars at night with his naked eye. About how many times more stars are there in the universe, compared to the stars a human can actually see?

Exercise 4

The estimated world population in 2011 was 7×10^9 . Of the total population, 682 million of those people were left-handed. Approximately what percentage of the world population is left-handed according to the 2011 estimation?

Exercise 5

The average person takes about 30,000 breaths per day. Express this number as a single-digit integer times a power of 10.

If the average American lives about 80 years (or about 30,000 days), how many total breaths will a person take in her lifetime?

Problem Set

1. The Atlantic Ocean region contains approximately 2×10^{16} gallons of water. Lake Ontario has approximately 8,000,000,000,000 gallons of water. How many Lake Ontarios would it take to fill the Atlantic Ocean region in terms of gallons of water?
2. US national forests cover approximately 300,000 square miles. Conservationists want the total square footage of forests to be $300,000^2$ square miles. When Ivanna used her phone to do the calculation, her screen showed the following:



- a. What does the answer on her screen mean? Explain how you know.
 - b. Given that the US has approximately 4 million square miles of land, is this a reasonable goal for conservationists? Explain. .
3. The average American is responsible for about 20,000 kilograms of carbon emission pollution each year. Express this number as a single-digit integer times a power of 10.
 4. The United Kingdom is responsible for about 1×10^4 kilograms. Which country is responsible for greater carbon emission pollution each year? By how much?

Lesson 9: Scientific Notation

Classwork

A positive, finite decimal s is said to be written in **scientific notation** if it is expressed as a product $d \times 10^n$, where d is a finite decimal so that $1 \leq d < 10$, and n is an integer.

The integer n is called the **order of magnitude** of the decimal $d \times 10^n$.

Are the following numbers written in scientific notation? If not, state why.

Exercise 1

$$1.908 \times 10^{17}$$

Exercise 4

$$4.0701 + 10^7$$

Exercise 2

$$0.325 \times 10^{-2}$$

Exercise 5

$$18.432 \times 5^8$$

Exercise 3

$$7.99 \times 10^{32}$$

Exercise 6

$$8 \times 10^{-11}$$